



**MAHARAJA SURAJMAL BRIJ UNIVERSITY
BHARATPUR**

SYLLABUS


M.SC. (MATHEMATICS)

(SEMESTER SCHEME)

BASED ON CHOICE BASED CREDIT SYSTEM (CBCS)

Academic Session 2023-24


(Mr. Munesh Kumar)


(Dr. Mahesh Kumar Jaiswal)


डॉ. अरुण कुमार पाण्डेय
उपकुलसचिव
प्रभारी अकादमिक प्रथम

M.Sc. Syllabus in Mathematics as per new scheme: credit- based semester system (four semester in two year) with continuous assessment [30% with non- inclusion in cumulative grade point average (CGPS)].

To obtain a Master's degree M.Sc. in Mathematics, a candidate is required to earn 120 credits with grade E or higher. For this each Semester will offer 36 credits. To earn credits for a paper, a candidate shall be required to obtain grade E or higher (or equivalent marks percentage) in the theory/practical examination. The candidate will not be permitted to appear in EoSE of a particular credit if he/she does not meet out 75% attendance requirement.

The Credit Courses have been classified as

- a) Compulsory Core Courses (CCC)
- b) Elective Core Courses (ECC)

A course is identified by a course code designated by a string of six alphanumeric characters and a course title. In a course code the first three characters of the string indicate the Department offering the course and the later three alphanumeric characters designate a particular course. In the case of compulsory core course the fourth character identifies the semester numeric digit and in case of the elective core courses the fourth character indicates the cluster of specialization. For compulsory or elective theory core courses the fifth character is '0' and for laboratory core course it is '1'.

Scheme of Examination –

The examination pattern comprises 50% internal assessment and 50% external assessment,


Internal Assessment

1. Internal examination/Periodic test will be consist of 30 marks in the mid of each semester.
2. The Student will submit two assignments form theory papers of the semester: each assignment will have 20 marks.
3. The Student will present seminar/tutorial of 30 marks in semester from each theory paper.

External Assessment

Theory Paper

1. Each theory paper in end-of-semester examination (EoSE) carries 100 marks.
2. The semester examination will be of 3 hours duration.


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3. The semester examination's question paper divided into two parts; Part 'A' and Part 'B'.
4. Part 'A' will be 20 marks and Part 'B' will be 80 marks.

Part 'A':

1. This section contains 10 short answer questions of 20 marks.
2. Questions will be based on knowledge, understanding and applications of the topic/texts covered in the syllabus.
3. Each question will carry two marks for correct answer.

Part 'B':

1. This section will consist of eight questions (two questions from each unit).
2. Students have to attempt any four questions. Each question carries equal marks.

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FIRST SEMESTER

S.No.	Paper Code	Paper Name	Paper Category	Credit	Contact Hours Per week	EoSE Duration (Hrs.)
1.	MAT 701	Algebra-I	CCC	6	6	3
2.	MAT 702	Real Analysis	CCC	6	6	3
3.	MAT 703	Differential Equation-I	CCC	6	6	3
4.	MAT 704	Differential Geometry	ECC	6	6	3
5.	MAT 705	Dynamics of Rigid Bodies	ECC	6	6	3
6.	MAT 706	Calculus of Variation and Special Function-I	ECC	6	6	3
Total Credit in the Semester				36		

SECOND SEMESTER

S.No.	Paper Code	Paper Name	Paper Category	Credit	Contact Hours Per week	EoSE Duration (Hrs.)
1.	MAT 801	Algebra-II	CCC	6	6	3
2.	MAT 802	Topology	CCC	6	6	3
3.	MAT 803	Differential Equation-II	CCC	6	6	3
4.	MAT 804	Riemannian Geometry and Tensor Analysis	ECC	6	6	3
5.	MAT 805	Hydrodynamics	ECC	6	6	3
6.	MAT 806	Special Function-II	ECC	6	6	3
Total Credit in the Semester				36		

EoSE: End of Semester Examination


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Elective Core Courses

Specialization Clusters

A.	CM	Continuum Mechanics
B.	BLT	Boundary layer theory
C.	MP	Mathematical Programming
D.	CGT	Combinatorics and Graph Theory
E.	RC	Relativity and Cosmology
F.	IM	Industrial Mathematics
G.	MHD	Magnetohydrodynamics
H.	NA	Numerical Analysis
I.	CA	Computer Application

Elective Course	Specialization	Paper	Prerequisite	Credit
MAT A01	CM	Continuum Mechanics - I	-----	6
MAT A02	CM	Continuum Mechanics - II	MAT A01	6
MAT B01	BLT	Boundary Layer Theory - I	-----	6
MAT B02	BLT	Boundary Layer Theory - II	MAT B01	6
MAT C01	MP	Mathematical Programming - I	-----	6
MAT C02	MP	Mathematical Programming - II	MAT C01	6
MAT D01	CGT	Combinatorics and Graph Theory - I	-----	6
MAT D02	CGT	Combinatorics and Graph Theory -II	MAT D01	6
MAT E01	RC	Relativistic Mechanics	-----	6
MAT E02	RC	General Relativity and Cosmology	MAT E01	6
MAT F01	IM	Industrial Mathematics - I	-----	6
MAT F02	IM	Industrial Mathematics - II	MAT F01	6
MAT G01	MHD	Magnetohydrodynamics - I	-----	6
MAT G02	MHD	Magnetohydrodynamics - II	MAT G01	6
MAT H01	NA	Numerical Analysis - I	-----	6
MAT H02	NA	Numerical Analysis -II	MAT H01	6
MAT I01	CA	Computer Application -Theory	-----	6
MAT I11	CA	Computer Application -Practical	MAT I01	6

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THIRD SEMESTER

S.No.	Paper Code	Paper Name	Paper Category	Credit	Contact Hours Per week	EoSE Duration (Hrs.)
1.	MAT 901	Functional Analysis -I	CCC	6	6	3
2.	MAT 902	Viscous Fluid Dynamics-I	CCC	6	6	3
3.	MAT 903	Integral Transforms	CCC	6	6	3
Candidates are required to opt any three elective core courses (6 credits each) from MAT A01, MAT B01, MAT C01, MAT D01, MAT E01, MAT F01, MAT G01, MAT H01, MAT I01.						
Total Credit in the Semester				36		

FOURTH SEMESTER

S.No.	Paper Code	Paper Name	Paper Category	Credit	Contact Hours Per week	EoSE Duration (Hrs.)
1.	MAT X01	Functional Analysis -II	CCC	6	6	3
2.	MAT X02	Viscous Fluid Dynamics-II	CCC	6	6	3
3.	MAT X03	Integral Equations	CCC	6	6	3
Candidates are required to opt the corresponding three elective core courses of same specialization cluster obtained in Semester third (6 credits each) from MAT A02, MAT B02, MAT C02, MAT D02, MAT E02, MAT F02, MAT G02, MAT H02, MAT I11.						
Total Credit in the Semester				36		

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M.Sc. Mathematics Syllabus
Semester I and II
Semester – I

Paper-1: MAT 701: Algebra-I

Max.Marks-100

Theory Paper

Unit-1

Direct product of groups (External and Internal). Isomorphism theorems – Diamond isomorphism theorem, Butterfly Lemma, Conjugate classes (Excluding p-groups). Sylow's theorems (without proof), Cauchy's theorem for finite abelian groups.

Unit – 2

Commutators, Derived subgroups. Normal series and Solvable groups, Composition series, Refinement theorem and Jordan-Holder theorem for infinite groups.

Unit -3

Polynomial rings and irreducibility criteria. Field theory – Extension fields, Algebraic and Transcendental extensions, Separable and inseparable extensions, Normal extensions. Splitting fields.

Unit -4

Galois theory – the elements of Galois theory, Automorphism of extensions, Fundamental theorem of Galois theory, Solutions of polynomial equations by radicals And Insolvability of general equation of degree five by radicals.

Reference Books:

1. Deepak Chatterjee, Abstract Algebra, Prentice Hall of India (PHI), New Delhi, 2004
2. N.S.Gopalkrishnan, University Algebra, New Age International, 1986.
3. Qazi Zameeruddin and Surjeet Singh, Modern Algebra, Vikas Publishing, 2006
4. G.C.Sharma, Modern Algebra, Shivalal Agrawal & Co., Agra, 1998.
5. Joseph A. Gallian, Contemporary Abstract Algebra (4th Ed.), Narosa Publishing House, 1999.
6. David S. Dummit and Richard M. Foote, Abstract Algebra (3rd Edition), John Wiley and Sons (Asia) Pvt. Ltd, Singapore, 2004.
7. . Stephen H. Friedberg, Arnold J. Insel, Lawrence E. Spence, Linear Algebra(4th Edition), Prentice-Hall of India Pvt. Ltd., New Delhi, 2004.
8. I.N. Herstein, Topics in Algebra (2nd edition), John Wiley & Sons, 2006.
9. Michael Artin, Algebra (2nd edition), Pearson Prentice Hall, 2011.


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Paper -2: MAT 702: Real Analysis

Theory Paper

Max.Marks-100

Unit – 1

Algebra and algebras of sets, Algebras generated by a class of subsets, Borel sets, Lebesgue measure of sets of real numbers, Measurability and Measure of a set, Existence of Non-measurable sets.

Unit – 2

Measurable functions, Realization of non-negative measurable function as limit of an Increasing sequence of simple functions, Structure of measurable functions, Convergence in measure, Egoroff's theorem

Unit-3

Weierstrass's theorem on the approximation of continuous function by polynomials, Lebesgue integral of bounded measurable functions, Lebesgue theorem on the passage to the limit under the integral sign for bounded measurable functions.

Unit – 4

Summable functions, Space of square summable functions. Fourier series and coefficients, Parseval's identity, Riesz-Fisher Theorem.

Reference Books:

1. Shanti Narayan, A Course of Mathematical Analysis, S. Chand & Co., N.D., 1995.
2. S.C.Malik and Savita Arora, Mathematical Analysis, New Age International, 1992.
3. T. M. Apostol, Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.
4. R.R. Goldberg, Real Analysis, Oxford & IBH Publishing Co., New Delhi, 1970.
5. S. Lang, Undergraduate Analysis, Springer-Verlag, New York, 1983.
6. Walter Rudin, Real and Complex Analysis, Tata McGraw-Hill Pub. Co. Ltd., 1986.
7. I.N. Natansen, Theory of Functions of a Real Variable, Fredrik Pub. Co., 1964.
8. G. de Barra, Measure theory and Integrations, New Age Publication (P) Ltd., New Delhi, 2014

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Paper-3: MAT 703: Differential Equations-I

Theory Paper

Max.Marks-100

Unit – 1

Non-linear ordinary differential equations of particular forms. Riccati's equation General solution and the solution when one, two or three particular solutions are Known.

Unit – 2

Total Differential equations. Forms and solutions, necessary and sufficient condition, Geometrical Meaning Equation containing three and four variables, total differential equations of second degree.

Unit – 3

Series Solution: Radius of convergence, method of differentiation, Cauchy-Euler Equation, Solution near a regular singular point (Method of Forbenius) for different cases, Particular integral and the point at infinity.

Unit – 4

Partial differential equations of second order with variable co-efficients- Monge's Method.

Reference Books:

1. J.L.Bansal and H.S.Dhami, Differential Equations Vol-II, JPH, 2004.
2. M.D. Raisinghanian, Ordinary and Partial Differential Equations, S. Chand & Co., 2003.
3. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Vol. 19, AMS, 1999.
4. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988.
5. E.A. Codrington, An Introduction to Ordinary Differential Equations, Prentice Hall of India, 1961.
6. Frank Ayres, Theory and Problems of Differential equations, TMH, 1990.
7. D.A. Murray, Introductory Course on Differential Equations, Orient Longman, 1902.
8. A.R.Forsyth, A Treatise on Differential Equations, Macmillan & Co. Ltd., London, 1956.
9. S.L. Ross, Differential Equations 2nd Edition John Willey & Sons, India 2007.

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Paper- 4: MAT 704: Differential Geometry

Max.Marks-100

Theory Paper

Unit – 1

Space curves, Tangent, Contact of curve and surface, Osculating plane, Principal normal and Binormal, Curvature, Torsion, Serret-Frenet's formulae, Osculating circle and Osculating sphere, Existence and Uniqueness theorems, Bertrand curves, Involute and Evolutes.

Unit – 2

Conoids, Inflexional tangents, Singular points, Indicatrix. Ruled surface, Developable surface, Tangent plane to a ruled surface. Necessary and sufficient condition that a surface $z = f(x, y)$ should represent a developable surface. Metric of a surface, First, Second and Third fundamental forms. Fundamental magnitudes of some important surfaces, Orthogonal trajectories.

Unit-3

Normal curvature. Principal directions and Principal curvatures, First curvature, Mean curvature, Gaussian curvature, Radius of curvature of a given section through any point on $z = f(x, y)$. Lines of curvature, Principal radii, Relation between fundamental forms.

Unit – 4

Asymptotic lines, Differential equation of an asymptotic line, Curvature and Torsion of an asymptotic line. Gauss's formulae, Gauss's characteristic equation, Weingarten equations, Mainardi-Codazzi equations. Fundamental existence theorem for surfaces, Parallel surfaces, Gaussian and mean curvature for a parallel surface.

Reference Books:

1. R.J.T. Bell, Elementary Treatise on Co-ordinate geometry of three dimensions, Macmillan India Ltd., 1994.
2. Mittal and Agarwal, Differential Geometry, Krishna publication, 2014.
3. Barry Spain, Tensor Calculus, Radha Publ. House Calcutta, 1988.
4. J.A. Thorpe, Introduction to Differential Geometry, Springer-Verlog, 2013.
5. T.J. Willmore An Introduction to Differential Geometry. Oxford University Press. 1972.
6. Weatherburn, Riemannian Geometry and Tensor Calculus, Cambridge Univ. Press, 2008.
7. Thorpe, Elementary Topics in Differential Geometry, Springer Verlag, N.Y. (1985).
8. R.S. Millman and G.D. Parker, Elements of Differential Geometry, Prentice Hall, 1977.

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Paper- 5: MAT 705: Dynamics of Rigid Bodies

Max.Marks-100

Theory Paper

Unit – 1

D'Alembert's principle. The general equations of motion of a rigid body. Motion of centre of inertia and motion relative to centre of inertia. Motion about a fixed axis.

Unit – 2

The compound pendulum, Centre of percussion. Conservation of momentum (linear and angular) and energy for finite as well as impulsive forces.

Unit – 3

Motion in three dimensions with reference to Euler's dynamical and geometrical equations. Motion under no forces, Motion under impulsive forces, Motion of a top,

Unit – 4

Lagrange's equations for holonomous dynamical system, Energy equation for conservative field, Small oscillations, Hamilton's equations of motion, Hamilton's principle and principle of least action.

Reference Books:

1. N. C. Rana and P.S. Joag, Classical Mechanics, Tata McGraw-Hill, 1991.
2. M. Ray and H.S. Sharma, A Text Book of Dynamics of a Rigid Body, Students' Friends & Co., Agra, 1984.
3. H. Goldstein, Classical Mechanics, Narosa, 1990. 4. J. L. Synge and B. A. Griffith, Principles of Mechanics, McGraw-Hill, 1991.
4. 5. L. N. Hand and J. D. Finch, Analytical Mechanics, Cambridge University Press, 1998.

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Paper -6: MAT 706: Calculus of Variation and Special Function-I
Theory Paper **Max.Marks-100**

Unit – 1

Calculus of variation – Functionals, Variation of a functional and its properties, Variational problems with fixed boundaries, Euler's equation, Extremals, Functional dependent on several unknown functions and their first order derivatives.

Unit-2

Functionals dependent on higher order derivatives, Functionals dependent on the function of more than one independent variable. Variational problems in parametric Form.

Unit-3

Gauss hypergeometric function and its properties, Series solution of Gauss hypergeometric equation. Integral representation, Linear and quadratic transformation formulas, Contiguous function relations, Differentiation formulae, Linear relation between the solutions of Gauss hypergeometric equation, Kummer's confluent hypergeometric function and its properties, Integral representation, Kummer's first transformation and series solution of Legendre's equation.

Unit – 4

Legendre polynomials and functions $P_n(x)$ and $Q_n(x)$.

Reference Books:

1. J.L.Bansal and H.S.Dhami, Differential Equations Vol-II, JPH, 2004.
2. M.D. Raisinghania, Ordinary and Partial Differential Equations, S. Chand & Co., 2003.
3. J.N.Sharma and R.K.Gupta, Differential Equations with Special Functions, Krishna Prakashan, 1991.
4. Earl D. Rainville, Special Functions, Macmillan Company, New York, 1960.
5. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Vol. 19, AMS, 1999.
6. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988.


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Semester – II

Paper-1: MAT 801 : Algebra II

Theory Paper

Max.Marks-100

Unit – 1

Linear transformation of vector spaces, Dual spaces, Dual basis and their properties, Dual maps, Annihilator.

Unit – 2

Matrices of linear maps, Matrices of composition maps, Matrices of dual map, Eigen values, Eigen vectors, Rank and Nullity of linear maps and matrices, Invertible matrices, Similar matrices.

Unit – 3

Determinants of matrices and their computations. Characteristic polynomial, minimal polynomial and eigen values. Real inner product space, Schwartz inequality.

Unit – 4

Orthogonality, Bessel's inequality, Adjoint, Self adjoint linear transformations and matrices, Orthogonal linear transformation and matrices, Principal Axis Theorem.

Reference Books:

1. Deepak Chatterjee, Abstract Algebra, Prentice Hall of India (PHI), New Delhi, 2004
2. N.S.Gopalkrishnan, University Algebra, New Age International, 1986.
3. Qazi Zameeruddin and Surjeet Singh, Modern Algebra, Vikas Publishing, 2006
4. G.C.Sharma, Modern Algebra, Shival Agrawal & Co., Agra, 1998.
5. Joseph A. Gallian, Contemporary Abstract Algebra (4th Ed.), Narosa Publishing House, 1999.
6. David S. Dummit and Richard M. Foote, Abstract Algebra (3rd Edition), John Wiley and Sons (Asia) Pvt. Ltd, Singapore, 2004.
7. Stephen H. Friedberg, Arnold J. Insel, Lawrence E. Spence, Linear Algebra (4th Edition), Prentice-Hall of India Pvt. Ltd., New Delhi, 2004.
8. I.N. Herstein, Topics in Algebra (2nd edition), John Wiley & Sons, 2006.
9. Michael Artin, Algebra (2nd edition), Pearson Prentice Hall, 2011.




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Paper-2: MAT 802: Topology

Max.Marks-100

Theory Paper

Unit – 1

Topological spaces, Subspaces, Open sets, Closed sets, Neighborhood system, Bases and sub-bases.

Unit – 2

Continuous mapping and Homeomorphism, Nets, Filters.

Unit – 3

Separation axioms (T_0 , T_1 , T_2 , T_3 , T_4). Compact and locally compact spaces. Continuity and Compactness.

Unit – 4

Product and Quotient spaces. One point compactification theorem. Connected and Locally connected spaces, Continuity and Connectedness.

Reference Books:

1. Shanti Narayan, A Course of Mathematical Analysis, S. Chand & Co., N.D., 1995.
2. S.C.Malik and Savita Arora, Mathematical Analysis, New Age International, 1992.
3. James R. Munkres, Topology, 2nd Edition, Pearson International, 2000.
4. J. Dugundji, Topology, Prentice-Hall of India, 1975.
5. George F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hill, 1963.

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Paper 3: MAT 803: Differential Equation-II

Max.Marks-100

Theory Paper

Unit – 1

Classification of linear partial differential equation of second order, Canonical forms, Cauchy's problem of first order partial differential equation.

Unit – 2

Linear homogeneous boundary value problem, Eigen values and eigen functions, Sturm-Liouville boundary value problems, orthogonality of eigen functions, Lagrange's identity, properties of eigen functions, important theorems of Sturm Liouville system, Periodic functions.

Unit – 3

Non-homogeneous boundary value problems, Non-homogeneous Sturm-Liouville boundary value problems (method of eigen function expansion). Method of separation of variables, Laplace, wave and diffusion equations.

Unit – 4

Green's Functions: Non-homogeneous Sturm-Liouville boundary value problem (method of Green's function), Procedure of constructing the Green's function and solution of boundary value problem, properties of Green's function, Inhomogeneous boundary conditions, Dirac delta function, Bilinear formula for Green's function, Modified Green's function.

Reference Books:

1. J.L.Bansal and H.S.Dhami, Differential Equations Vol-II, JPH, 2004.
2. M.D. Raisinghania, Ordinary and Partial Differential Equations, S. Chand & Co., 2003.
3. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Vol. 19, AMS, 1999.
4. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988.
5. E.A. Codington, An Introduction to Ordinary Differential Equations, Prentice Hall of India, 1961.
6. Frank Ayres, Theory and Problems of Differential equations, TMH, 1990.
7. D.A. Murray, Introductory Course on Differential Equations, Orient Longman, 1902.
8. A.R.Forsyth, A Treatise on Differential Equations, Macmillan & Co. Ltd., London, 1956.
9. T. Myint -U, Ordinary Differential Equations, Elsevier North -Holland, 1978

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Paper-4: MAT 804: Riemannian Geometry and Tensor Analysis

Theory Paper

Max.Marks-100

Unit – 1

Geodesics, Differential equation of a geodesic, Single differential equation of a geodesic, Geodesic on a surface of revolution, Geodesic curvature and torsion, Gauss- Bonnet Theorem.

Unit – 2

Tensor Analysis- Kronecker delta. Contravariant and Covariant tensors, Symmetric tensors, Quotient law of tensors, Relative tensor. Riemannian space. Metric tensor, Indicator, Permutation symbols and Permutation tensors.

Unit -3


Christoffel symbols and their properties, Covariant differentiation of tensors. Ricci's theorem, Intrinsic derivative, Geodesics, Differential equation of geodesic, Geodesic coordinates, Field of parallel vectors.

Unit – 4

Reimann-Christoffel tensor and its properties. Covariant curvature tensor, Einstein space. Bianchi's identity. Einstein tensor, Flat space, Isotropic point, Schur's theorem.

Reference Books:

1. R.J.T. Bell, Elementary Treatise on Co-ordinate geometry of three dimensions, Macmillan India Ltd., 1994.
2. Mittal and Agarwal, Differential Geometry, Krishna publication, 2014.
3. Barry Spain, Tensor Calculus, Radha Publ. House Calcutta, 1988.
4. J.A. Thorpe, Introduction to Differential Geometry, Springer-Verlog, 2013.
5. T.J. Willmore An Introduction to Differential Geometry. Oxford University Press. 1972.
6. Weatherburn, Reimanian Geometry and Tensor Clculus, Cambridge Univ. Press, 2008.
7. Thorpe, Elementary Topics in Differential Geometry, Springer Verlag, N.Y. (1985).
8. R.S. Millman and G.D. Parker, Elements of Differential Geometry, Prentice Hall, 1977.


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Paper-5: MAT 805: Hydrodynamics

Theory Paper

Max.Marks-100

Unit – 1

Kinematics of ideal fluid. Lagrange's and Euler's methods. Equation of continuity in Cartesian, cylindrical and spherical polar coordinates. Boundary surface. Stream-lines, path-lines and streak lines, velocity potential, irrotational motion.

Unit – 2

Euler's hydrodynamic equations, Bernoulli's theorem. Helmholtz equations. Cauchy's Integral.

Unit-3

Motion due to impulsive forces. Motion in two-dimensions, Stream function, Complex potential. Sources, Sinks, Doublets, Images in two-dimensions.


Unit – 4

Vortex motion definition, rectilinear vortices, centre of vortices, properties of vortex tube, two vortex filaments, vortex pair, vortex doublet, vortex inside and outside circular cylinder, four vortices, motion of vortex situated at the origin and stream lines.

Reference Books:

1. M.D. Raisinghania, Hydrodynamics, S. Chand & Co. Ltd., N.D. 1995.
2. M. Ray and G.C. Chadda, A Text Book on Hydrodynamics, Students' Friends & Co., Agra, 1985.
3. N. C. Rana and P.S. Joag, Classical Mechanics, Tata McGraw-Hill, 1991.
4. H. Goldstein, Classical Mechanics, Narosa, 1990.
5. J. L. Synge and B. A. Griffith, Principles of Mechanics, McGraw-Hill, 1991.
6. L. N. Hand and J. D. Finch, Analytical Mechanics, Cambridge University Press, 1998.


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Paper-6: MAT 806: Special Functions- II

Theory Paper

Max.Marks-100

Unit – 1

Bessel functions $J_n(x)$.

Unit -2

Hermite polynomials $H_n(x)$, Laguerre and Associated Laguerre polynomials.

Unit – 3

Jacobi Polynomial: Definition and its special cases, Bateman's generating function, Rodrigue's formula, orthogonality, recurrence relations, expansion in series of Polynomials.

Unit – 4

Chebyshev polynomials $T_n(x)$ and $U_n(x)$: Definition, Solutions of Chebyshev's equation, expansions, Generating functions, Recurrence relations, Orthogonality.

Reference Books:

1. J.L.Bansal and H.S.Dhami, Differential Equations Vol-II, JPH, 2004.
2. M.D. Raisinghanian, Ordinary and Partial Differential Equations, S. Chand & Co., 2003.
3. J.N.Sharma and R.K.Gupta, Differential Equations with Special Functions, Krishna Prakashan, 1991.
4. Earl D. Rainville, Special Functions, Macmillan Company, New York, 1960.
5. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Vol. 19, AMS, 1999.
6. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988.



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प्रभारी अकादमिक प्रथम

M.Sc. Mathematics
Semester Scheme (Semester III and IV)
Semester - III

Paper-1: MAT 901:Functional Analysis- I

Max.Marks-100

Theory Paper

Unit 1:

Subspace of a metric space, Product space, Continuous mappings, Sequence in a metric space, Convergent, Cauchy sequence. Complete metric space.

Unit-2

Banach contraction theorem, Baire's category theorem, compact sets, compact spaces, Separable metric space and connected metric spaces.

Unit -3


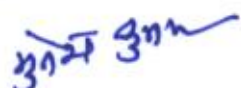
Normed linear spaces. Quotient space of normed linear spaces and its completeness. Banach spaces and examples. Bounded linear transformations. Normed linear space of bounded linear transformations.

Unit – 4

Equivalent norms. Basic properties of finite dimensional normed linear spaces and compactness. Reisz Lemma. Multilinear mapping. Open mapping theorem. Closed graph theorem. Uniform boundness theorem.

Reference Books:

1. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley and Sons., 1978.
2. A. E. Taylor, Introduction to Functional Analysis, John Wiley, 1958.
3. A. Bowers and N. Kalton, An Introductory Course in Functional Analysis, Springer Verlag, 2014.
4. W. Rudin, Functional Analysis, McGraw-Hill, 1973.


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Paper-2: MAT 902 : Viscous Fluid Dynamics-I

Max.Marks-100

Theory Paper

Unit - 1

Viscosity, Analysis of stress and rate of strain, Stoke's law of friction, Thermal conductivity and generalized law of heat conduction, Equations of state and continuity, Navier-Stokes equations of motion.

Unit-2

Vorticity and circulation, Dynamical similarity, Inspection and dimensional analysis, Buckingham theorem and its application, Non-dimensional parameters and their physical importance: Reynolds number, Froude number, Mach number, Prandtl number, Eckart number, Grashoff number, Brinkmann number, Non dimensional coefficients: Lift and drag coefficients, Skin friction, Nusselt number, Recovery factor.

Unit-3

Exact solutions of Navier-Stokes equations, Velocity distribution for plane couette flow, Plane Poiseuille flow, Generalized plane Couette flow, Hagen- Poiseuille flow, Flow in tubes of uniform cross-sections.

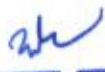
Unit - 4

Flow between two concentric rotating cylinders. Stagnation point flows: Hiemenz flow, Homann flow. Flow due to a rotating disc.

Reference Books:

1. J.L. Bansal, Viscous Fluid dynamics, JPH, Jaipur, 2008.
2. M.D.Raisinghania, Fluid Dynamics, S.Chand, 2003.
3. F. Chorlton, A Text Book of Fluid Dynamics, CBC, 1985.
4. S. W. Yuan, Foundations of Fluid Mechanics, Prentice-Hall, 1976.
5. S. I. Pai, Viscous Flow Theory I- Laminar Flow, D. Van Nostrand Co., Inc., Princeton, New Jersey, N.Y., Landon, Toronto, 1956.
6. F.M.White, Viscous Fluid Flow, McGraw-Hill, N.Y., 1974.


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Paper -3: MAT 903: Integral Transforms

Theory Paper

Max.Marks-100

Unit - 1

Fourier transform - Definition and properties of Fourier sine, cosine and complex transforms. Convolution theorem. Inversion theorems. Fourier transform of derivatives.

Unit-2

Mellin transform- Definition and elementary properties. Mellin transforms of derivatives and integrals, Inversion theorem. Convolution theorem.

Unit - 3

Laplace transform- Definition and its properties. Rules of manipulation. Laplace transform of derivatives and integrals. Properties of inverse Laplace transform. Convolution theorem.

Unit - 4

Complex inversion formula. Infinite Hankel transform- Definition and elementary properties. Hankel transform of derivatives. Inversion theorem. Parseval Theorem.

Reference Books:

1. Lokenath Debnath and Dambaru Bhatta, Integral Transforms and their Applications, Taylor and Francis Group, 2014.
2. Abdul J. Jerry, Introduction to Integral Equations with applications, Marcel Dekkar Inc. NY, 1999.
3. L.G.Chambers, Integral Equations: A short Course, Int. Text Book Company Ltd. 1976.
4. Murry R. Spiegel, Laplace Transform (SCHAUM Outline Series), McGraw-Hill, 1965.

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Optional Papers: (ECC)

Paper - 4: MAT A01: Continuum Mechanics –I

Theory Paper

Max.Marks-100

Unit 1:

Cartesian Tensors, Index notation and transformation laws of Cartesian tensors. Addition, Subtraction and Multiplication of cartesian tensors, Gradient of a scalar function, Divergence of a vector function and Curl of a vector function using the index notation. E-8 identity. Conservative vector field and concept of a scalar potential function. Stokes, Gauss and Green's theorems.

Unit 2:

Continuum approach, Classification of continuous media, Body forces and surface forces. Components of stress tensor, Force and Moment equations of equilibrium. Transformation law of stress tensor. Stress quadric. Principal stress and principal axes. Stress invariants and stress deviator. Maximum shearing stress.

Unit 3:

Lagrangian and Eulerian description of deformation of flow. Comoving derivative, Velocity and Acceleration. Continuity equation. Strain tensors. Linear rotation tensor and rotation vector, Analysis of relative displacements.

Unit-4

Geometrical meaning of the components of the linear strain tensor, Properties of linear strain tensors. Principal axes, Theory of linear strain. Linear strain components. Rate of strain tensors. The vorticity tensor. Rate of rotation vector and vorticity, Properties of the rate of strain tensor, Rate of cubical dilation.

Reference Books:

1. W. Prager, Introduction to Mechanics of Continua, Lexington Mass, Ginn, 1961.
2. A.C. Eringen, Mechanics of Continua, Wiley, 1967.
3. T.J. Chung, Continuum Mechanics, Prentice-Hall, 1988.




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Paper-5: MAT B01: Boundary Layer Theory- I

Theory Paper

Max.Marks-100

Unit 1

Derivation of boundary layer equations for two-dimensional flow. Boundary layer along a flat plate (Blasius-Topfer solution). Characteristic boundary layer parameters. Similar solutions.

Unit - 2

Exact solution of the steady state boundary layer equations in two-dimensional flow. Flow past a wedge. Flow along the wall of a convergent channel. Boundary layer separation.

Unit-3

Flow past a symmetrically placed cylinder (Blasius series solution). Gortler new series method. Plane free jet, Circular jet, Plane wall jet. Prandtl-Mises transformation and its application of plane free jet.

Unit - 4

Axially symmetrical boundary layers on bodies at rest. Boundary layers on a body of revolution. Mangler's transformation. Three-dimensional boundary layers - Boundary layer flow on yawed cylinder. Growth of three-dimensional boundary layer on a rotating disc impulsively set in motion.

Reference Books:

1. J.L. Bansal, Viscous Fluid dynamics, JPH, Jaipur, 2008.
2. M.D.Raisinghania, Fluid Dynamics, S.Chand, 2003.
3. F. Chorlton, A Text Book of Fluid Dynamics, CBC, 1985.
4. S. W. Yuan, Foundations of Fluid Mechanics, Prentice-Hall, 1976.
5. S. I. Pai, Viscous Flow Theory I- Laminar Flow, D. Van Nostrand Co., Inc., Princeton, New Jersey, N.Y., Landon, Toronto, 1956.
6. F.M.White, Viscous Fluid Flow, McGraw-Hill, N.Y., 1974.


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Paper-6: MAT C01: Mathematical Programming -I

Theory Paper

Max.Marks-100

Unit - 1

Separating and supporting hyperplane theorems. Revised simplex method to solve Linear Programming problems, Bounded variable problems.

Unit-2

Integer programming: Gomory's algorithm for all and mixed integer programming problems, Branch and Bound algorithm; Goal programming: Graphical goal attainment method, Simplex method for GPP.

Unit - 3

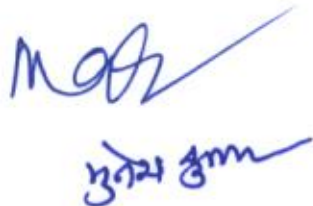
Separable programming: Piece-wise Linear approximations to non-linear functions, Reduction to separable programming problem to l.p.p., separable programming algorithm, fractional programming: computational procedure.

Unit – 4

Dynamic programming: Introduction, Bellman principle of optimality, solution of problems with finite number stages, solution of l.p.p. by dynamic programming.

Reference Books:

1. Kanti Swaroop, P.K.Gupta and Manmohan, Operation Research, Sultan Chand & Sons., N.Delhi, 2007.
2. S.D.Sharma, Operations Research, Kedar Nath Ram Nath and co. Meerut, 2005.
3. F. S. Hillier and G. J. Lieberman, Introduction to Operations Research
1. Concepts and Cases (9th Edition), Tata McGraw Hill, 2010.
2. 4 Hamdy A. Taha, Operations Research, An Introduction (9th edition), Prentice-Hall, 2010.
4. G. Hadley, Linear Programming, Narosa Publishing House, New Delhi, 2002.




:: रूप कुमार पाण्डेय
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Paper-7: MAT D01: Combinatorics and Graph Theory-I

Theory Paper

Max.Marks-100

Unit - 1

Introduction to digraph, Orientation of a graph, Underlying graph, Parallel edges, Source and Sink, Types of digraphs, Accessibility, Arborescence, Spanning arborescence, Euler digraphs, Handshaking dilemma, Incidence matrix of a digraph, Circuit matrix of a digraph.

Unit - 2

Degree sequences, Graphic sequence, Havel Hakimi Theorem. Matrix representation of graphs except adjacency and incidence matrix.

Unit - 3

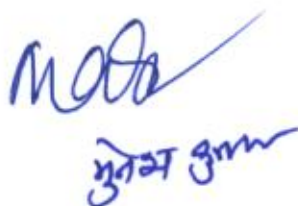
Planar graphs Kuratowski's graphs, Maximal planar graphs, Outer planar graphs, Maximal outer planar graph, Minimally non-outer planar graph, Thickness and Crossing number of bipartite and complete bipartite graph, Euler's formula, Kuratowski's theorem.

Unit - 4

Isomorphism, Homomorphism. Graph theory in Network analysis Network flows, Transport networks, Max-flow min-cut-theorem.

Reference Books:

1. N. Deo, Graph Theory, Prentice Hall of India, New Delhi, 2004.
2. C.Vasudev, Graph theory and it application, New Age International Pvt., 2006,
3. N.L. Biggs, Discrete Mathematics, Oxford Science Publication, 1985.
4. T. Koshy, Discrete Mathematics with Applications, Academic Press, 2005.


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Paper-8: MAT E01: Relativistic Mechanics Teaching

Theory Paper

Max.Marks-100

Unit - 1

Relative Character of space and time, Principle of Relativity and its postulates, Derivation of special Lorentz transformation equations, Composition of Parallel velocities, Lorentz-Fitzgerald contraction formula, Time dilation.

Unit - 2

Simultaneity, Relativistic transformation formulae for velocity, Lorentz contraction factor, Particle acceleration, Velocity of light as fundamental velocity, Relativistic aberration and its deduction to Newtonian theory.

Unit - 3

Variation of mass with velocity, Equivalence of mass and energy, Transformation formulae for mass, Momentum and energy, Problems on conservation of mass, Momentum and energy, Relativistic Lagrangian and Hamiltonian.

Unit - 4

Minkowski space, Space-like, Time-like and Light-like intervals, Null cone, Relativity and Causality, Proper time, World line of a particle. Principles of Equivalence and General Covariance.

Reference Books:

1. J.V. Narlikar, Lectures on General Relativity and Cosmology, Macmillan Co. Ltd. India, N.Delhi, 1978.
2. C. Moller, The Theory of Relativity, Oxford Clarendon Press, 1952.
3. P.G. Bergmann, Introduction to the Theory of Relativity, Prentice Hall of India, 1969.
4. J.L. Anderson, Principles of Relativity Physics, Academic Press, 1967.
5. W. Rindler, Essential Relativity, Van Nostrand Reinhold Company, 1969.
6. V. A. Ugarov, Special Theory of Relativity, Mir Publishers, 1979.


मुकुन्द गुप्ता


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Paper-9: MAT F01: Industrial Mathematics- I

Theory Paper

Max.Marks-100

Unit -1

Partial differential equations and techniques of solution. Finite difference methods for solving PDE. Application to problems of industry with special reference to Fluid Mechanics.

Unit -2

Operational Techniques. Linear Programming problems. Computational procedure of Simplex method, Two-phase Simplex method, Big-M-method.

Unit - 3

Revised Simplex method, Duality in linear programming, Duality and Simplex method.

Unit - 4

Assignment models. Mathematical formulation, Hungarian method. Travelling Salesman problem. Transportation models. Mathematical formulation. Initial basic feasible solution. Degeneracy and unbalanced transportation problems.

Reference Books:

1. Kanti Swaroop, P.K.Gupta and Manmohan, Operation Research, Sultan Chand & Sons., N.Delhi, 2007.
2. S.D.Sharma, Operations Research, Kedar Nath Ram Nath and co. Meerut, 2005.
3. H.A.Taha, Operations Research: An Introduction; MacMillan Publishing Company, New York, 1982.
4. F.S. Hillier and G.J. Lieberman, Introduction to Operations Research; Holden Day, 1962.
5. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988.


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Paper-10: MAT G01: Magnetohydrodynamics - I

Theory Paper

Max.Marks-100

Unit -1

Maxwell electromagnetic field equations. Constitutive equations of fluid motion, Stokes hypothesis. Maxwell stress tensor. Fundamental Magnetofluid-dynamics. equations of

Unit - 2

Magnetofluiddynamic approximations. Magnetic field equation, Frozen in fluid,

Unit 3

number, Magnetic parameter, Magnetic Prandtl number and Nusselt number.


Alfven transverse waves. MHD boundary conditions. Inspection and Dimensional analysis, π -products. Reynolds number, Mach number, Prandtl number, Magnetic Reynolds number, Magnetic pressure number, Hartmann

Unit 4

Hartmann plane Poiseuille flow and plane Couette flow including temperature distribution. MHD flow in a tube of rectangular cross-section. MHD pipe flow. MHD flow in annular channel. MHD flow between two rotating coaxial cylinders.

Reference Books:

1. J.L.Bansal, Magnetofluidynamics of Viscous Fluids, JPH, Jaipur, 1994.
2. K.R. Cramer and S.I.Pai, Magnetofluidynamics for Enginners and Applied Physicists, McGraw-Hill, N.Y., 1973.
3. P.A. Davidson, An Introduction to Magnetohydrodynamics, Cambridge Univ. Press, U.K., 2001.
4. J.A.Shercliff, A Textbook of Magnetohydrodynamics, Pergamon Press., 1965.
5. K.R. Cramer and S.I. Pai, Magnetofluid Dynamics for Engineers and Applied Physicists, McGraw-Hill Book Co., 1973.


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Paper - 11: MAT H01: Numerical Analysis - I

Theory Paper

Max.Marks-100

Unit - 1

Iterative methods - Theory of iteration method, Acceleration of the convergence, Chebyshev method, Muler's method, Methods for multiple and complex roots

Unit 2

Newton-Raphson method for simultaneous equations, Convergence of iteration process in the case of several unknowns. Solution of polynomial equations - Polynomial equation, Real and complex roots, Synthetic division, the Birge-Vieta, Bairstow and Graeffe's root squaring method.

Unit-3


System of simultaneous Equations (Linear)- Direct method, Method of determinant, Gauss-Jordan, LU-Factorizations-Doolittle's, Crout's and Cholesky's. Partition method. Relaxation methods.

Unit - 4

Eigen value problems- Basic properties of eigen values and eigen vector, Power methods, Method for finding all eigen values of a matrix. Jacobi, Givens' and Rutishauser method. Complex eigen values.

Reference Books:

1. S.S.Sastry, Introductory Methods of Numerical Analysis, PHI, 1979.
2. V.Rajaraman, Computer Oriented Numerical Methods, PHI, 1993.
3. M.K.Jain, S.R.K. Eyenger and R.K. Jain, Numerical Methods for Mathematics and Applied Physicists, Wiley-Eastern Pub., N.Delhi, 2005.
4. B. Bradie, A Friendly Introduction to Numerical Analysis, Pearson Education, India, 2007.
5. C. F. Gerald and P. O. Wheatley, App;ied Numerical Analysis, Pearson Education, India, 7th edition, 2008.
6. C.F. Gerald, P.O. Wheatley, Applied Numerical Analysis, Addison-Wesley, 1998.
7. S. D. Conte, C de Boor, Elementary Numerical Analysis, McGraw-Hill, 1980.
8. C.E. Froberg, Introduction to Numerical Analysis, (Second Edition), Addition-Wesley, 1979.


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Paper-12: MAT 101: Computer Applications- Theory

Theory Paper

Max.Marks-100

Unit - 1

Introduction to computers, Computer organization, Input-output devices, Memory system. Hardware and software. Operating system.

Unit - 2

Computer languages, System software and application software. Windows: Graphical user interface, control panel and all features there in files and folders management. Using Accessories, Getting help, copying, moving and sharing information between programs. Setting up printer and fonts. Configuring modem. Introduction to MS Word and Ms-Excel. Algorithms and flow charts. Programming languages and problem solving on computers.

Unit 3:

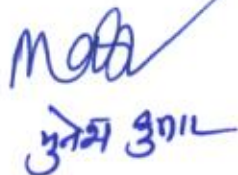
Programming using Matlab/Mathematica/Maple Variables, Vector and - Matrix Computation, Built-in-functions, Plotting, output, M-files.

Unit 4:

Programming using Matlab/Mathematica/Maple Functions, Loops, Conditional Execution, Matrix Multiplication.

Reference Books:

1. Y. Kanetkar, Let Us C, BPB Publications, 2008.
2. C. Ghezzi and M. Jazayeri, Programming Languages Concepts, John Wiley, 1977.
3. M. Marcotty & H.F. Ledgard, Programming Language Landscape, Galgotia Publication, 1981.
4. B.S. Gottfried, Schaum's Outline of Theory and Problems of Programming with C, McGraw-Hill, 1996.
5. Brian R. Hunt, Ronald L. Lipsman, Jonathan M. Rosenberg, A Guide to MATLAB, Cambridge Univ. Press, 2001.
6. Duane hanselman and Bruce Littlefield, Mastering Matlab-7, Pearson Education 2005,
7. William J. Palm III, Introduction to Matlab-7 for Engineers, McGraw Hill, 2005.
8. Mureşan, Marian, Introduction to Mathematica® with Applications, Springer, 2017.
9. José Guillermo Sánchez León, Mathematica Beyond Mathematics: The Wolfram Language in the Real World, Chapman and Hall/CRC, 2017.


म. अ. क. सिंग


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Semester - IV

Paper -I MAT X01: Functional Analysis II and Advanced Calculus

Theory Paper

Max.Marks-100

Unit - 1

Continuous linear functionals. Hahn-Banach theorem and its consequences. Embedding and Reflexivity of normed spaces. Dual spaces with examples. Inner product spaces.

Unit - 2

Hilbert space and its properties. Cauchy-Schwartz inequality, Orthogonality and Functionals in Hilbert Spaces. Pythagorean theorem, Projection theorem, Separable Hilbert spaces and Examples.

Unit - 3


Orthonormal sets, Bessel's inequality, Existence of orthonormal bases by Gram- schmidt orthogonalization process. Complete orthonormal sets, Parseval's identity, Structure of a Hilbert space, Riesz representation theorem, Reflexivity of Hilbert spaces.

Unit - 4

Adjoint of an operator on a Hilbert space. Self-adjoint, Positive, Normal and Unitary operators and their properties. Projection on a Hilbert space. Invariance. Reducibility. Orthogonal projections. Eigen values and eigen vectors of an operator. Spectrum of an operator Spectral theorem.

Reference Books:

1. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley and Sons., 1978.
2. A. E. Taylor, Introduction to Functional Analysis, John Wiley, 1958.
3. A. Bowers and N. Kalton, An Introductory Course in Functional Analysis, Springer Verlag, 2014.
4. W. Rudin, Functional Analysis, McGraw-Hill, 1973.


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Paper-2: MAT X02: Viscous Fluid Dynamics - II

Theory Paper

Max.Marks-100

Unit - 1

Concept of unsteady flow, Flow due to plane wall suddenly set in the motion (Stokes' first problem), Flow due to an oscillating plane wall (Stokes' second problem), Starting flow in plane Couette motion, Suction/injection through porous wall.

Unit - 2

Equation of energy, Temperature distribution: Between parallel plates, in a pipe, between two concentric rotating cylinders.

Unit -3

Variable viscosity plane Couette flow, temperature distribution of plane Couette flow with transpiration cooling. Theory of very slow motion: Stokes' and Oseen's flows past a sphere.

Unit - 4

Concept of boundary layer, Derivation of velocity and thermal boundary equations in two-dimensional flow. Boundary layer on flat plate (Balsius-Topfer solution), Simple solution of thermal boundary layer equation for $Pr=1$.

Reference Books:

1. J.L. Bansal, Viscous Fluid dynamics, JPH, Jaipur, 2008.
2. M.D.Raisinghania, Fluid Dynamics, S.Chand, 2003.
3. F. Chorlton, A Text Book of Fluid Dynamics, CBC, 1985.
4. S. W. Yuan, Foundations of Fluid Mechanics, Prentice-Hall, 1976.
5. S. I. Pai, Viscous Flow Theory I- Laminar Flow, D. Van Nostrand Co., Inc., Princeton, New Jersey, N.Y., Landon, Toronto, 1956.
6. F.M.White, Viscous Fluid Flow, McGraw-Hill, N.Y., 1974.


पुणे २१ डिसेंबर


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Paper-3: MAT X03: Integral Equations

Theory Paper

Max.Marks-100

Unit - 1

Linear integral equations- Definition and classification. Conversion of initial and boundary value problems to an integral equation. Eigen values and Eigen functions. Solution of homogeneous and general Fredholm integral equations of second kind with separable kernels.

Unit - 2

Solution of Fredholm and Volterra integral equations of second kind by methods of successive substitutions and successive approximations. Resolvent kernel and its results. Conditions of uniform convergence and uniqueness of series solution.

Unit-3


Integral equations with symmetric kernels Orthogonal system of functions. Fundamental properties of eigen values and eigen functions for symmetric kernels. Expansion in eigen functions and bilinear form. Hilbert-Schmidt theorem. Solution of Fredholm integral equations of second kind by using Hilbert-Schmidt theorem.

Unit - 4

Solution of Volterra integral equations of second kind with convolution type kernels by Laplace transform. Solution of singular integral equations by Fourier transform. Classical Fredholm theory- Fredholm theorems. Solution of Fredholm integral equation of second kind by using Fredholm first theorem.

Reference Books:

1. Shanti Swarup, Integral Equations, Krishna Publications, Meerut.
2. M.D.Raisinghania, Integral Equations and Boundary Value Problems, S.Chand, 2010.
3. Abdul J. Jerry, Introduction to Integral Equations with applications, Marcel Dekkar Inc. NY, 1999.
4. L.G.Chambers, Integral Equations: A short Course, Int. Text Book Company Ltd. 1976.


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Optional Paper (ECC)

Paper 4: MAT A02: Continuum Mechanics - II

Theory Paper

Max.Marks-100

Unit - 1

Law of conservation of mass and Eulerian continuity equation. Reynolds transport theorem. Momentum integral theorem and equation of motion.

Unit-2

Kinetic equation of state. First and the second law of thermodynamics and dissipation function. Applications (Linear elasticity and Fluids) - Assumptions and basic equations. Generalized Hook's law for an isotropic homogeneous solid.

Unit-3


Compatibility equations (Beltrami-Michell equations). Classification of types of problems in linear elasticity. Principle of superposition, Strain energy function, Uniqueness theorem, p-p relationship and work kinetic energy equation, Irrotational flow and Velocity potential.


Unit - 4

Kinetic equation of state and first law of Thermodynamics. Equation of continuity. Equations of motion. Vorticity-stream surfaces for inviscid flow, Bernoulli's equations. Irrotational flow and velocity potential. Similarity parameters of fluid flow.

Reference Books:

1. W. Prager, Introduction to Mechanics of Continua, Lexington Mass, Ginn, 1961.
2. A.C. Eringen, Mechanics of Continua, Wiley, 1967.
3. T.J. Chung, Continuum Mechanics, Prentice- Hall, 1988.


गुप्त गुप्त


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Paper-5: MAT B02: Boundary Layer Theory - II

Theory Paper

Max.Marks-100.

Unit-1

Unsteady boundary layers Method of successive approximations, Boundary layer growth after impulsive start of motion and in accelerated motion, Boundary layer for periodic flow (Pulsatile pressure gradient).

Unit - 2

Approximate methods for the solution of the boundary layer equations. Karman momentum integral equation. Karman-Pohlhausen method and its application. Waltz- Thwaites method. Energy integral equation.

Unit - 3


Derivation of two-dimensional thermal boundary layer equation for flow over a plane wall. Forced convection in a laminar boundary layer on a flat plate, Crocco's first and second integrals. Reynolds analogy.

Unit - 4

Temperature distribution in the spread of a jet (i) Plane free jet, (ii) Circular jet (iii) Plane wall jet. Free convection from a heated vertical plate. Thermal-energy integral equation. Approximate solution of the Pohlhausen's problem of free convection from a heated vertical plate.

Reference Books:

1. J.L. Bansal, Viscous Fluid dynamics, JPH, Jaipur, 2008.
2. M.D.Raisinghania, Fluid Dynamics, S.Chand, 2003.
3. F. Chorlton, A Text Book of Fluid Dynamics, CBC, 1985.
4. S. W. Yuan, Foundations of Fluid Mechanics, Prentice-Hall, 1976.
5. S. I. Pai, Viscous Flow Theory I- Laminar Flow, D. Van Nostrand Co., Inc., Princeton, New Jersey, N.Y., Landon, Toronto, 1956.
6. F.M.White, Viscous Fluid Flow, McGraw-Hill, N.Y., 1974.


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Paper - 6: MAT C02 : Mathematical Programming - II

Theory Paper

Max.Marks-100

Unit - 1

Convex function, Quadratic forms, constrained problem of maxima and minima, Lagrangian method, Non-linear programming: Formulation and Graphical method.

Unit-2

Non-linear programming and its fundamental ingredients, Khun-Tucker necessary and sufficient conditions; Saddle point, Saddle-point theorems.

Unit - 3

Quadratic Programming: Kuhn-Tucker conditions, Wolfe method, Duality in Quadratic Programming.

Unit - 4

Beals method to solve QPP, Geometric Programming: Formulation, geometric arithmetic inequality, necessary conditions of optimality.

Reference Books:

1. Kanti Swaroop, P.K.Gupta and Manmohan, Operation Research, Sultan Chand & Sons., N.Delhi, 2007.
2. S.D.Sharma, Operations Research, Kedar Nath Ram Nath and co. Meerut, 2005.
3. F. S. Hillier and G. J. Lieberman, Introduction to Operations Research Concepts and Cases (9th Edition), Tata McGraw Hill, 2010.
4. Hamdy A. Taha, Operations Research, An Introduction (9th edition), Prentice-Hall, 2010.
5. G. Hadley, Linear Programming, Narosa Publishing House, New Delhi, 2002.


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Paper-7: MAT D02: Graph Theory-II

Theory Paper

Max.Marks-100

Unit - 1

Cut set and Cut vertices, Cut set and bridge, fundamental cut sets, Connectivity and Severability, Vector spaces of graphs.

Unit -2

Coloring: Graph coloring, Vertex coloring, Edge coloring, Properly coloring of a graph, Chromatic polynomial, Decomposition theorem, Four colour theorem, The five colour theorem.

Unit -3


Enumeration of graphs: Types of enumeration, Labeled graphs, Counting labeled trees, Rooted labeled trees, Enumeration of graphs, Partitions, Generating functions, Counting unlabeled trees, Rooted unlabeled trees, Permutation, Composition of permutation, Pólya's theorem, Burnside's lemma, Pólya's enumeration theorem


Unit - 4

Graph and Algorithms: Applications Shortest path algorithms, Dijkstra's algorithm, Algorithm for minimal spanning tree, Kruskal's algorithm, Prim's algorithm, The labeling algorithm

Reference Books:

1. K.H. Rosen, Discrete Mathematics and it's Applications, McGraw Hill, 1999.
2. C.Vasudev, Graph theory and it application, New Age International Pvt., 2006.
3. N.L. Biggs, Discrete Mathematics, Oxford Science Publication, 1985.
4. T. Koshy, Discrete Mathematics with Applications, Academic Press,
5. 2005. 5. N. Deo, Graph Theory, Prentice Hall of India, New Delhi, 2004.


पुणे २०१८


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Paper - 8: MAT E02: General Relativity & Cosmology

Theory Paper

Max.Marks-100

Unit - 1

Mach's principle, Newtonian approximation of equation of motion, Einstein's field equation for matter and empty space, Reduction of Einstein's field equation to Poisson's equation, Removal of clock paradox in General Relativity.

Unit - 2

Schwarzschild exterior metric, its isotropic form, Singularity and singularities in Schwarzschild exterior metric, Derivation of the formula GM/c^2 , Mass of sun in gravitational unit, Relativistic differential equation for the orbit of the planet.

Unit-3


Three crucial tests in General Relativity and their detailed descriptions, Analogues of Kepler's laws in General Relativity, Trace of Einstein tensor, Energy-momentum tensor and its expression for perfect fluid, Schwarzschild interior metric and boundary condition.

Unit - 4

Lorentz invariance of Maxwell's equations in empty space, Lorentz force on charged particle, Energy-momentum tensor for electro-magnetic field. Einstein's field equation with cosmological term, Static cosmological models (Einstein & de-Sitter models) with physical and geometrical properties, Non-static form of de-Sitter line- element and Red shift in this metric, Einstein space, Hubble's law, Weyl's postulate.

Reference Books:

1. J.V. Narlikar, Lectures on General Relativity and Cosmology, Macmillan Co. Ltd. India, N.Delhi, 1978.
2. C. Moller, The Theory of Relativity, Oxford Clarendon Press, 1952.
3. P.G. Bergmann, Introduction to the Theory of Relativity, Prentice Hall of India, 1969.
4. J.L. Anderson, Principles of Relativity Physics, Academic Press, 1967.
5. W. Rindler, Essential Relativity, Van Nostrand Reinhold Company, 1969.
6. V. A. Ugarov, Special Theory of Relativity, Mir Publishers, 1979.


प्रमुख अति


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Paper-9: MAT F02 : Industrial Mathematics - II

Theory Paper

Max.Marks-100.

Unit - 1

Inventory Models. EOQ models with and without shortages.

Unit - 2

EOQ models with constraints.

Unit-3

Replacement and Reliability models. Replacement of items that deteriorate, Replacement of items that fail completely.

Unit-4

Reliability Theory Coherent structure, Reliability of systems of independent components, Bounds on system reliability, Shapes of the system reliability function, Motion of aging, Parametric families of life distribute with Monotone failure rate.

Reference Books:

1. Kanti Swaroop, P.K.Gupta and Manmohan, Operation Research, Sultan Chand & Sons., N.Delhi, 2007.
2. S.D.Sharma, Operations Research, Kedar Nath Ram Nath and co. Meerut, 2005.
3. H.A.Taha, Operations Research: An Introduction; MacMillan Publishing Company, New York, 1982.
4. F.S. Hillier and G.J. Leiberman, Introduction to Operations Research; Holden Day, 1962.
5. I.N. Sneddon, Elements of Partial Differential Equations, McGraw-Hill, 1988


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Paper - 10: MAT G02: Magnetohydrodynamics - II

Theory Paper

Max.Marks-100

Unit - 1

MHD flow near a stagnation point. MHD Reyleigh's flow. MHD Stoke's flow past a sphere, MHD Oseen's flow past a sphere.

Unit - 2

MHD boundary layer flow past a flat plate in an aligned magnetic flow. Wilson's numerical solution technique. MHD boundary layer flow past a flat plate in a transverse magnetic field. modified Rossow's method of solution.

Unit - 3

MHD plane free jet flow. Wave and theory of characteristics, Equation of the characteristics, Characteristic surfaces, MHD characteristic equations. MHD waves.


Unit - 4

Friedrichs diagrams. Dispersion relation. MHD shock waves. Generalized Hugoniot condition. Compressive nature of MHD shocks. MHD shock wave classification. MHD shock stability.

Reference Books:

1. J.L.Bansal, Magnetofluidynamics of Viscous Fluids, JPH, Jaipur, 1994.
2. K.R. Cramer and S.L.Pai, Magnetofluidynamics for Enginners and Applied Physicists, McGraw-Hill, N.Y., 1973.
3. P.Á. Davidson, An Introduction to Magnetohydrodynamics, Cambridge Univ. Press, U.K., 2001.
4. J.A.Shercliff, A Textbook of Magnetohydrodynamics, Pergamon Press, 1965.
5. K.R. Cramer and S.I. Pai, Magnetofluid Dynamics for Engineers and Applied Physicists, McGraw-Hill Book Co., 1973.


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Paper-11: MAT H02: Numerical Analysis - II

Theory Paper

Max.Marks-100.

Unit - 1

Curve Fitting and Function Approximations - Least square error criterion. Linear regression. Polynomial fitting and other curve fittings, Approximation of functions by Taylor series and Chebyshev polynomials.

Unit -2

Numerical solution of Ordinary differential Equations - Taylor series Method, Picard method, Runge-Kutta methods upto fourth order, Multistep method (Predictor- corrector strategies).

Unit -3

Stability analysis Single and Multistep methods. BVP's of ordinary differential Equations - Boundary value problems (BVP's), Shooting methods.

Unit - 4


Finite difference methods. Difference schemes for linear boundary value problems of the type $y = f(x, y)$, $y' = f(x, y, y')$ and $y'' = f(x, y)$.

Reference Books:

1. S.S.Sastry, Introductory Methods of Numerical Analysis, PHI, 1979.
2. V.Rajaraman, Computer Oriented Numerical Methods, PHI, 1993.
3. M.K.Jain, S.R.K. Eyenger and R.K. Jain, Numerical Methods for Mathematics and Applied Physicists, Wiley-Eastern Pub., N.Delhi, 2005.
4. B. Bradie, A Friendly Introduction to Numerical Analysis, Pearson Education, India, 2007.
5. C. F. Gerald and P. O. Wheatley, Applied Numerical Analysis, Pearson. Education, India, 7th edition, 2008.
6. C.F. Gerald, P.O. Wheatley, Applied Numerical Analysis, Addison-Wesley, 1998.
7. S. D. Conte, C de Boor, Elementary Numerical Analysis, McGraw-Hill, 1980.
8. C.E. Froberg, Introduction to Numerical Analysis, (Second Edition), Addison-Wesley, 1979.


मुनेश कुमार

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Paper - 12: MAT 111: Computer Applications- Practical

Practical Paper

Max.Marks-100

Note:- There shall be five practicals with internal choice and candidates are required to attempt all give practicals.

Solution of system of linear equations - Gauss elimination, Gauss-Seidel, Eigenvalues and Eigenvectors Power method and inverse power method. Least Squares Approximation Fitting of straight line, parabola and cubic equation. Numerical integration - Trapezoidal and Simpson's methods, Differential equations and graphics: Double integration, Roots of polynomial, two and three dimensional plots, Numerical solution of Initial value problems - Euler's method, Fourth order Runge-Kutta method, solution of Boundary value problems by using inbuilt functions of MATLAB/Mathematica/Maple.

Distribution of Marks:

Five Practicals -	15 Marks each	75 Marks
Practical Record		10 Marks
Viva-Voce		15 Marks
Total Marks		100 Marks

Note:-

1. Each candidate is required to appear in the Practical examination to be conducted by internal and external examiners. External examiner will be appointed by the University through BOS and internal examiner will be appointed by the Head of the Department/Principal of the College.

2. Each candidate has to prepare his/her practical record.


मुख्य अध्येक्षक


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